



K24U 4019

Reg. No. :

Name :

**First Semester B.Sc. Degree (C.B.C.S.S. – OBE-Supplementary/
Improvement) Examination, November 2024**

(2019 to 2023 Admission)

CORE COURSE IN MATHEMATICS

1B01MAT : Set Theory, Differential Calculus and Numerical Methods

Time : 3 Hours

Max. Marks : 48

PART – A

Answer **four** questions from this part. **Each** question carries **one** mark. **(4×1=4)**

1. Define a relation in a set of all lines in a plane.
2. Find $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$.
3. Find all first partial derivative of the function $w = x^3yz + xy + y^5z$.
4. Find the domain and range of exponential function.
5. State Euler's theorem for homogeneous functions.

PART – B

Answer **any eight** questions from this part. **Each** question carries **two** marks. **(8×2=16)**

6. Find all the partition of the set $\{1, 2, 3\}$.
7. Show that the relation congruent modulo m is an equivalence relation on set of all integers.
8. Give an example of a function, which is not one-one, but on-to.
9. Locate the smallest positive root of the equation $f(x) = \tan x - 2x$.
10. If $2 - x^2 \leq g(x) \leq 2 \cos x$ for all x , find $\lim_{x \rightarrow 0} g(x)$.
11. Find all the values of x for which $x^3 - 3x = 1$.

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12. Show that $\lim_{\theta \rightarrow 0} \sin \theta = 0$.
13. At what points (x, y) in the plane are the function $f(x, y) = \sin \frac{1}{xy}$ is continuous.
14. The plane $x = 1$ intersects the paraboloid $z = x^2 + y^2$ in a parabola. Find the slope of the tangent to the parabola at $(1, 2, 5)$.
15. If $w = \sin(x + ct)$, show that $\frac{\partial^2 w}{\partial t^2} = c^2 \frac{\partial^2 w}{\partial x^2}$.
16. Draw a branch diagram and write a Chain Rule formula for derivative $\frac{dz}{dt}$ for $z = f(x, y)$, $x = g(t)$, $y = h(t)$.

PART – C

Answer **any four** questions from this part. **Each** question carries **four** marks.

(4×4=16)

17. Consider the function $f : A \rightarrow B$, $g : B \rightarrow C$, if both f and g are one-one then prove that if $g \circ f$ is one-one.
18. Define constant function. Find the number of constant functions from A to B .
19. Find the continuous extension of $f(x) = \frac{\sin x}{x}$.
20. If $y = \sin(\sin x)$, prove that $\frac{d^2 y}{dx^2} + \tan x \frac{dy}{dx} + y \cos^2 x = 0$.
21. Let $f(x, y) = \begin{cases} 0 & xy \neq 0 \\ 1 & xy = 0 \end{cases}$.
- a) Find the limit of f as (x, y) approaches $(0, 0)$ along the line $y = x$.
- b) Prove that f is not continuous at the origin.
22. Define homogeneous equation of degree n . Check whether the function $f(x, y) = x^3 \sin\left(\frac{y}{x}\right)$ is homogeneous or not.
23. Express $\frac{\partial w}{\partial r}$, and $\frac{\partial w}{\partial s}$ in terms of r and s if $w = x + 2y + z^2$,
 $x = \frac{r}{s}$, $y = r^2 + \ln s$, $z = 2r$.



PART – D

Answer **any two** questions from this part. **Each** question carries **six** marks. (2×6=12)

24. i) Find the domain of g and a formula for the inverse of $g(x) = \frac{2x-3}{5x-7}$.

ii) a) find $\log_2 64$, b) find $\log_{10} 0.001$

25. Find the root correct to two decimal places of the equation $xe^x = \cos x$, using the method of false position.

26. Find the n^{th} derivative of $\frac{1}{x^2 + a^2}$.

27. Show that $f(x, y) = \begin{cases} \frac{2xy}{x^2 + y^2} & \text{if } (x, y) \neq 0 \\ 0 & \text{if } (x, y) = 0 \end{cases}$ is continuous at every point except the origin.

